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MATHEMATICS

0580/43

Paper 4 (Extended)

May/June 2023

2 hours 30 minutes

You must answer on the question paper.

You will need: Geometrical instruments

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For π , use either your calculator value or 3.142.

INFORMATION

- The total mark for this paper is 130.
- The number of marks for each question or part question is shown in brackets [].

This document has **20** pages.

- 1 (a) Tomas sells a computer, a bike and a phone.
The amounts he receives are in the ratio computer : bike : phone = 14 : 17 : 9.
- (i) Calculate the amount he receives for the phone as a percentage of the total.

..... % [2]

- (ii) The total amount he receives is \$560.

Calculate how much he receives for the bike.

\$ [2]

- (iii) Tomas originally bought the bike for \$195.
He wanted to make a profit of at least 25% when he sold it.

Does Tomas make a profit of at least 25%?
You must show all your working to support your decision.

- (b) Ulla invests \$725 for 6 years in an account paying simple interest at a rate of 1.3% per year. [3]
- Calculate the total interest earned at the end of 6 years.

\$ [2]

- (c) In a sale, all prices are reduced by 24%.
Victor pays \$36.86 for a pair of shoes in the sale.

Calculate the original price of the shoes.

\$ [2]

- 2 (a) Anna records the number of text messages she receives for 14 days.

| | | | | | | |
|----|----|----|----|----|----|----|
| 17 | 15 | 31 | 38 | 31 | 22 | 13 |
| 18 | 21 | 27 | 28 | 21 | 31 | 29 |

- (i) Complete the stem-and-leaf diagram.

| | |
|---|--|
| 1 | |
| 2 | |
| 3 | |

Key:

[3]

- (ii) Find the median.

..... [1]

- (iii) Find the mode.

..... [1]

- (iv) Find the range.

..... [1]

- (b) In a shop, there are 4 red and 8 grey phones.
Anna and Pete each pick one of these phones at random.

Work out the probability that they both pick a grey phone.

..... [2]

- 3 (a) The scale drawing shows two sides, AB and BC , of a field.
The scale is 5 centimetres represents 200 metres.



Scale: 5 cm to 200 m

- (i) Measure angle ABC .

Angle $ABC = \dots\dots\dots$ [1]

- (ii) X is a point on BC .
 $BX = 332$ m.

Mark the point X on the diagram. [2]

- (iii) Find the scale in the form $1 : n$.

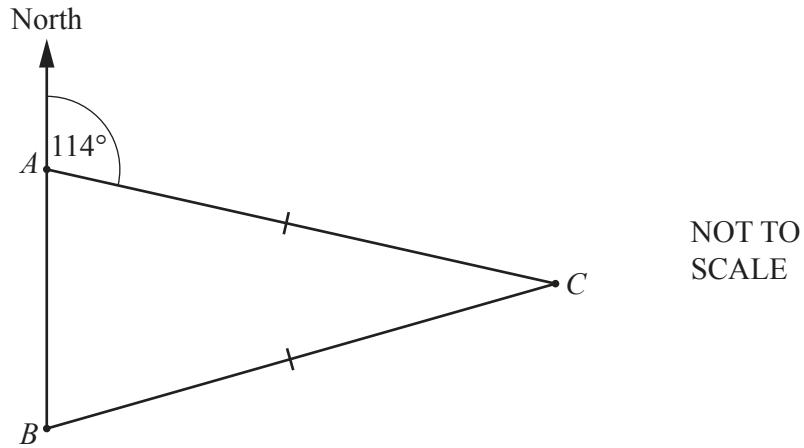
1: $\dots\dots\dots$ [2]

- (b) A bronze statue is 4.5 m high and has a mass of 195 200 kg.
The density of bronze is 8000 kg/m^3 .
The volume of a mathematically similar model of the statue is 0.385 m^3 .

Calculate the height of the model.
[Density = Mass \div Volume]

$\dots\dots\dots$ m [5]

4 (a)

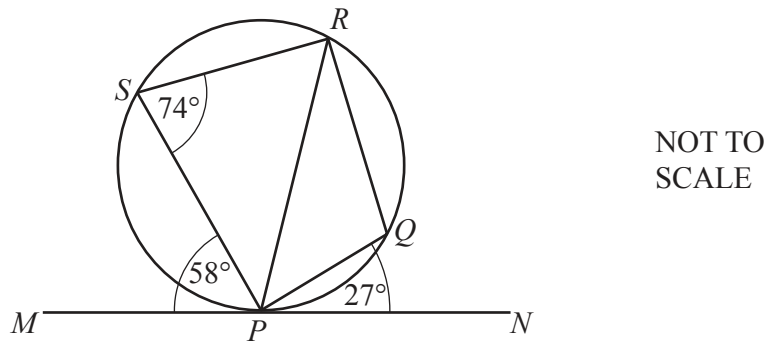


A , B and C are three towns and the bearing of C from A is 114° .
 B is due south of A and $AC = BC$.

Calculate the bearing of B from C .

..... [3]

(b)



P , Q , R and S lie on a circle.
 MPN is a tangent to the circle at P .
 Angle $MPS = 58^\circ$, angle $PSR = 74^\circ$ and angle $QPN = 27^\circ$.

(i) Find angle PRS .

Angle $PRS =$ [1]

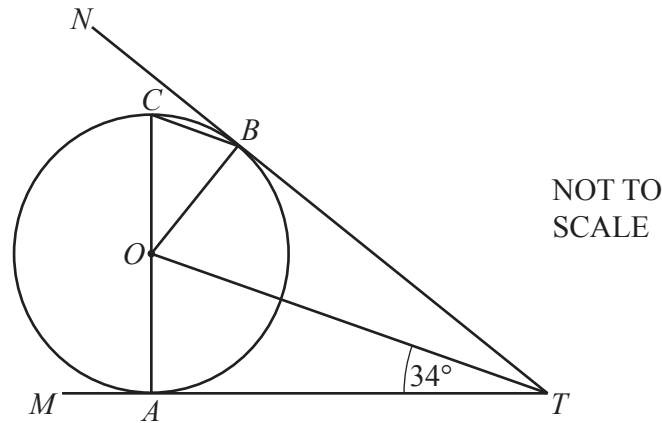
(ii) Find angle PQR .

Angle $PQR =$ [1]

(iii) Find angle RPQ .

Angle $RPQ =$ [2]

(c)



A , B and C lie on a circle, centre O , with diameter AC .
 TAM and TBN are tangents to the circle and angle $ATO = 34^\circ$.

Using values and geometrical reasons, complete these statements to show that CB is parallel to OT .

In triangles AOT and BOT , OT is common.

Angle $OAT = \text{angle } OBT = 90^\circ$ because

.....

$AT = BT$ because

.....

Triangle AOT is congruent to triangle BOT because of congruence criterion

Angle $AOT = \text{angle } BOT = 56^\circ$ because angles in a triangle add up to 180° .

Angle $BOC = \dots\dots\dots^\circ$ because

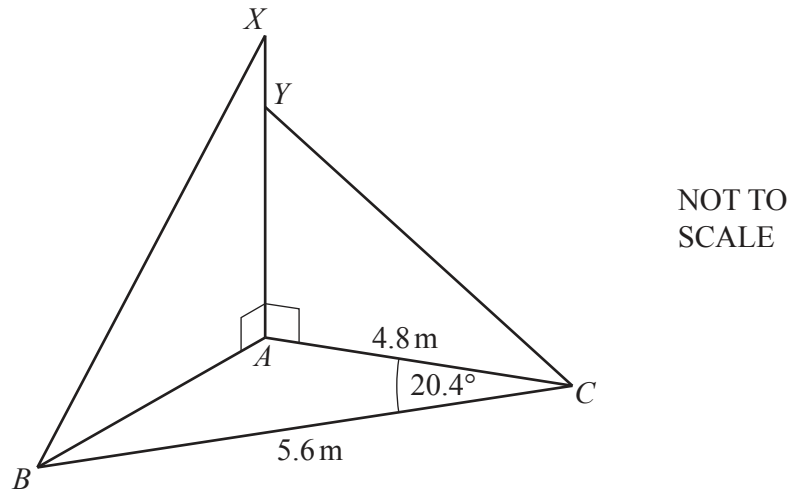
Angle $OBC = \dots\dots\dots^\circ$ because

.....

CB is parallel to OT because

[6]

5 (a)



ABC is a scalene triangle on horizontal ground.

AYX is a straight vertical post, held in place by two straight wires XB and YC .

$AC = 4.8$ m, $BC = 5.6$ m and angle $ACB = 20.4^\circ$.

(i) Calculate AB .

$AB = \dots\dots\dots$ m [3]

(ii) Angle $XBA = 64^\circ$.

Calculate AX .

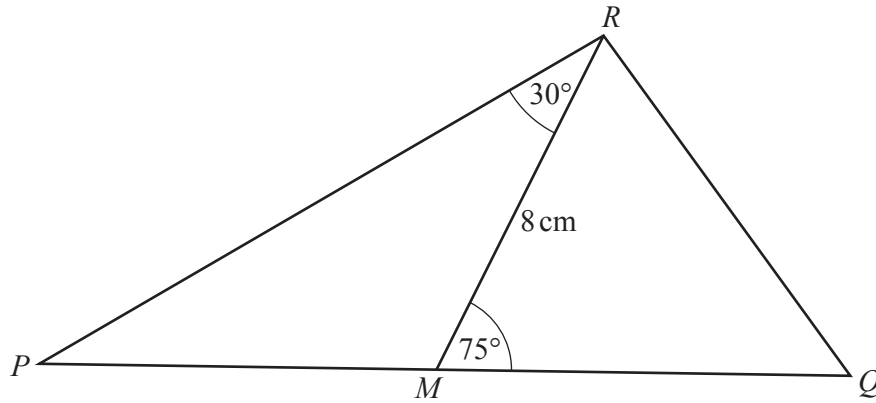
$AX = \dots\dots\dots$ m [2]

(iii) $AY = 2.9$ m.

Calculate the area of triangle YAC .

$\dots\dots\dots$ m² [2]

(b)

NOT TO
SCALE

In triangle PQR , M is the midpoint of PQ .
 $RM = 8\text{ cm}$, angle $PRM = 30^\circ$ and angle $RMQ = 75^\circ$.

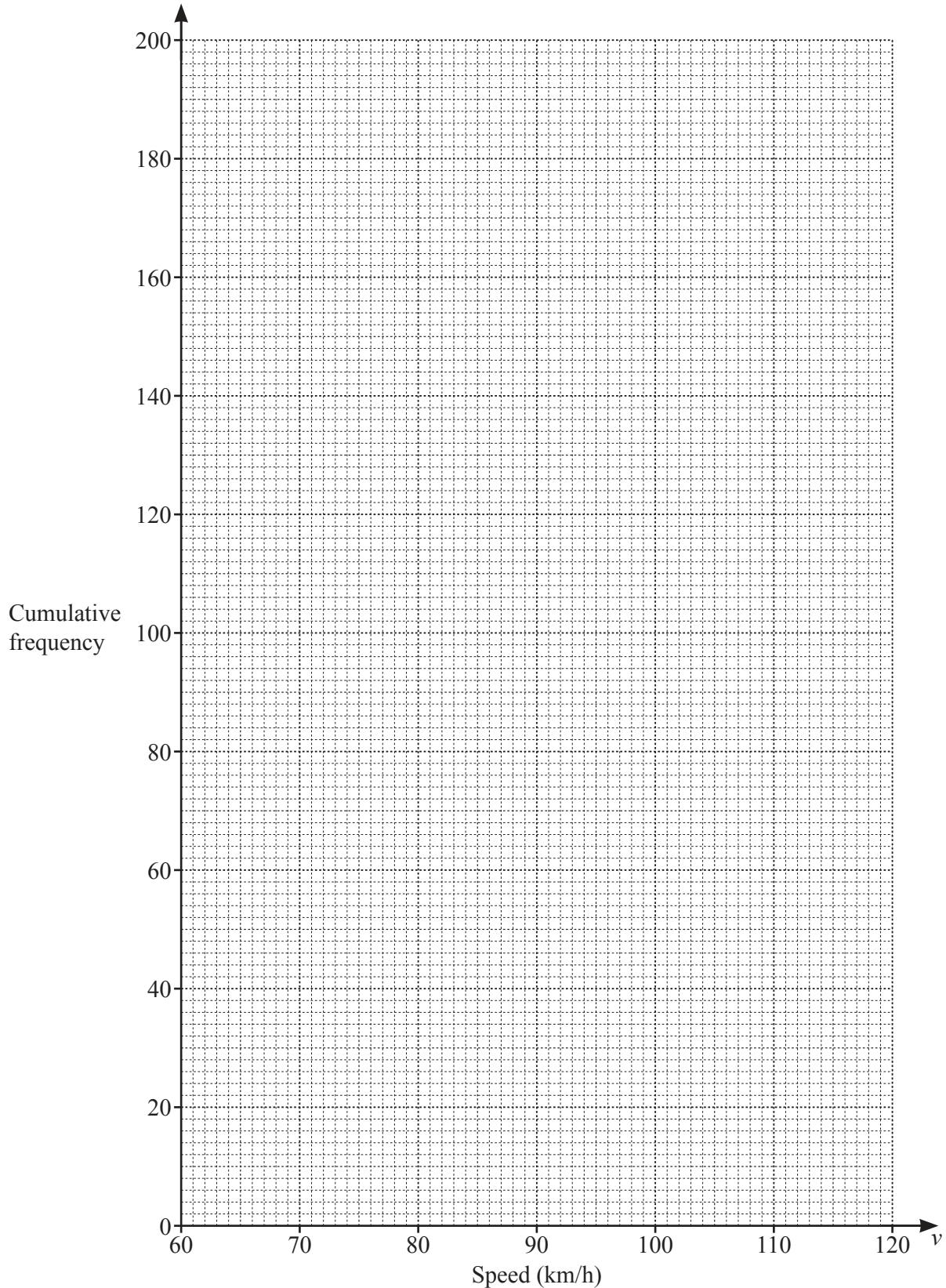
Calculate PQ .

$PQ = \dots\dots\dots\text{ cm [5]}$

- 6 (a) The cumulative frequency table shows information about the speed of each of 200 cars as they pass a speed camera.

| Speed (v km/h) | $v \leq 70$ | $v \leq 80$ | $v \leq 90$ | $v \leq 95$ | $v \leq 100$ | $v \leq 120$ |
|----------------------|-------------|-------------|-------------|-------------|--------------|--------------|
| Cumulative frequency | 12 | 46 | 115 | 155 | 177 | 200 |

- (i) On the grid, draw the cumulative frequency diagram.



(ii) Use your cumulative frequency diagram to find an estimate of

(a) the median

..... km/h [1]

(b) the interquartile range

..... km/h [2]

(c) the number of cars with a speed greater than 110 km/h.

..... [2]

(b) The frequency table shows information about the mass of each of 50 trucks.

| Mass (m kg) | $2000 < m \leq 2600$ | $2600 < m \leq 3500$ | $3500 < m \leq 5000$ | $5000 < m \leq 5700$ |
|-------------------|----------------------|----------------------|----------------------|----------------------|
| Frequency | 12 | 15 | 16 | 7 |

(i) Calculate an estimate for the mean mass of the trucks.

..... kg [4]

(ii) In a histogram showing this information, the height of the first block is 6 cm.

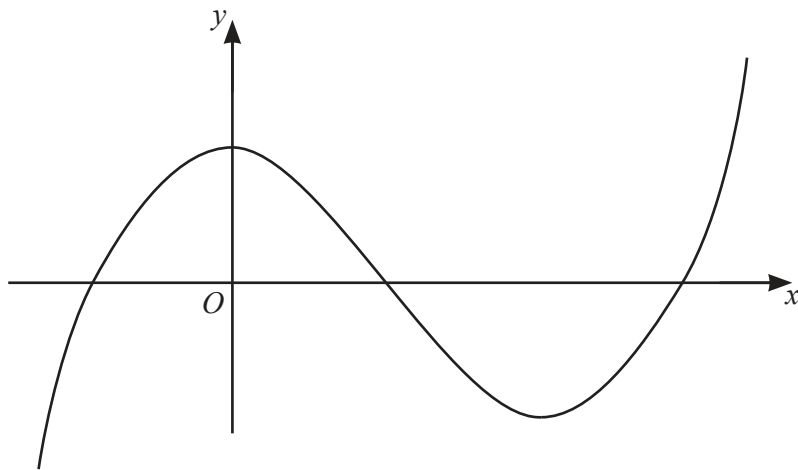
Calculate the heights of the remaining three blocks.

Height of block for $2600 < m \leq 3500$ cm

Height of block for $3500 < m \leq 5000$ cm

Height of block for $5000 < m \leq 5700$ cm [3]

- 7 (a) The diagram shows the graph of a function.

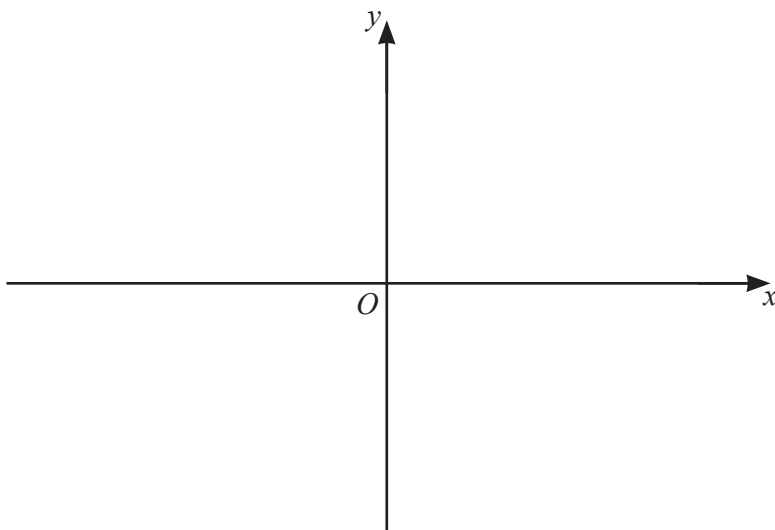


Put a ring around the word which correctly identifies the type of function.

reciprocal quadratic cubic exponential linear

[1]

- (b) (i)



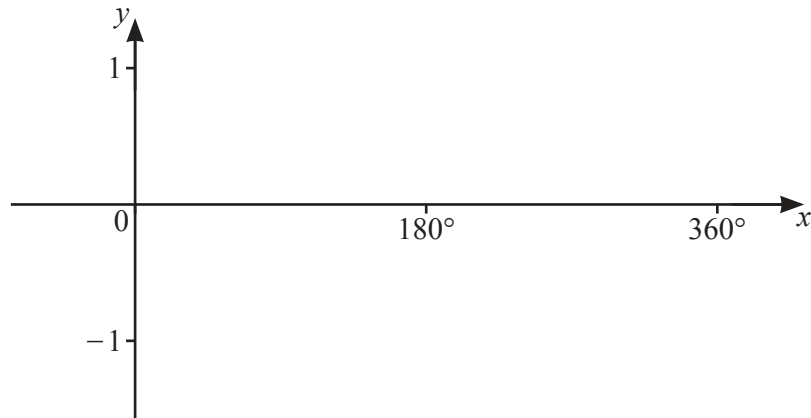
On the diagram, sketch the graph of $y = \frac{1}{2x}$, $x \neq 0$.

[2]

- (ii) Solve the equation $\frac{1}{2x} = 2x$.

$x = \dots\dots\dots$ and $x = \dots\dots\dots$ [2]

(c) (i)



On the diagram, sketch the graph of $y = \sin x$ for $0^\circ \leq x \leq 360^\circ$. [2]

(ii) Solve the equation $3 \sin x + 1 = 0$ for $0^\circ \leq x \leq 360^\circ$.

$x = \dots\dots\dots$ and $x = \dots\dots\dots$ [3]

- 8 (a) A shop sells shirts for \$ x and jackets for \$ $(x + 27)$.
The shop sells 4 shirts and 3 jackets for a total of \$194.75 .

Write down and solve an equation to find the cost of one shirt.

\$ [3]

- (b) Solve the simultaneous equations.
You must show all your working.

$$\begin{aligned}x^2 + 4y &= 37 \\ 5x + y &= -8\end{aligned}$$

$x = \dots\dots\dots$, $y = \dots\dots\dots$

$x = \dots\dots\dots$, $y = \dots\dots\dots$ [5]

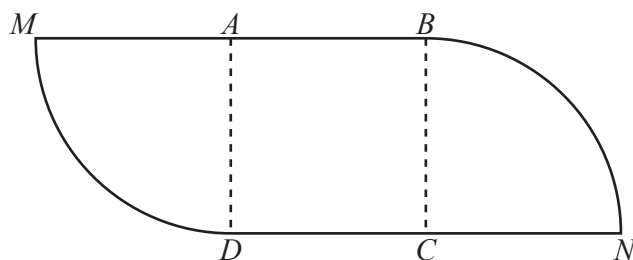
- (c) A solid cylinder has radius x and height $6x$.
A sphere of radius r has the same surface area as the total surface area of the cylinder.

Show that $r^2 = \frac{7}{2}x^2$.

[The surface area, A , of a sphere with radius r is $A = 4\pi r^2$.]

[4]

9 (a)

NOT TO
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The diagram shows a shape made from a square $ABCD$ and two equal sectors of a circle.
The square has side 11 cm.
 MAB and DCN are straight lines.

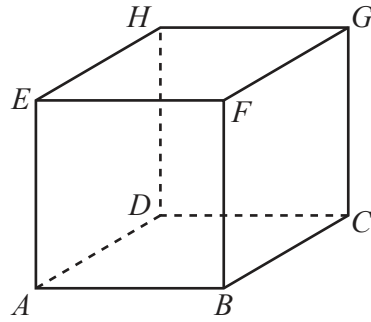
(i) Calculate the area of the shape.

..... cm^2 [3]

(ii) Calculate the perimeter of the shape.

..... cm [3]

(b)

NOT TO
SCALE

The diagram shows a cube $ABCDEFGH$ of edge 7 cm.

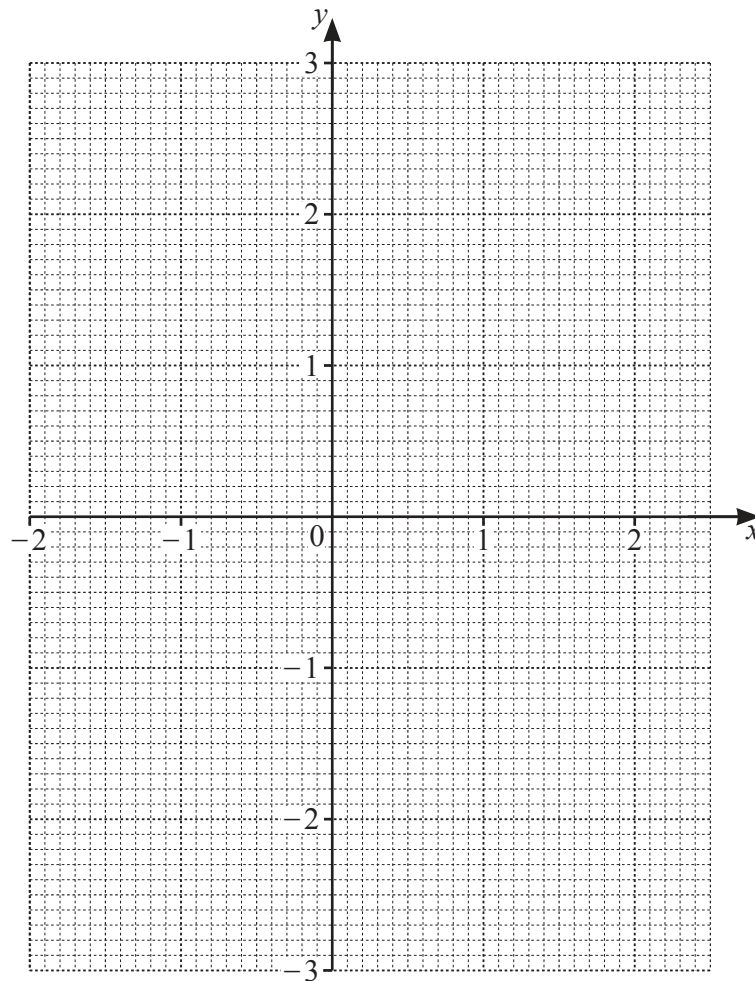
Calculate the angle between AG and the base of the cube.

..... [4]

- 10 The table shows some values for $y = 2^x - 3$.

| | | | | | | | | |
|-----|-------|----|---|-------|---|-------|---|------|
| x | -2 | -1 | 0 | 0.5 | 1 | 1.5 | 2 | 2.5 |
| y | -2.75 | | | -1.58 | | -0.17 | 1 | 2.66 |

- (a) Complete the table. [3]
- (b) On the grid, draw the graph of $y = 2^x - 3$ for $-2 \leq x \leq 2.5$.



[4]

- (c) Use your graph to solve the equation $2^x - 3 = 2$.

$x = \dots\dots\dots$ [1]

- (d) By drawing a suitable straight line, solve the equation $2^x - x - 1.5 = 0$.

$x = \dots\dots\dots$ or $x = \dots\dots\dots$ [4]

11 M has coordinates $(4, 1)$ and N has coordinates $(-2, -7)$.

(a) Find the length of MN .

..... [3]

(b) Find the gradient of MN .

..... [2]

(c) Find the equation of the perpendicular bisector of MN .

..... [4]

Question 12 is printed on the next page.

12 The equation of a curve is $y = x^4 - 8x^2 + 5$.

- (a) Find the derivative, $\left(\frac{dy}{dx}\right)$, of $y = x^4 - 8x^2 + 5$.

..... [2]

- (b) Find the coordinates of the three turning points.
You must show all your working.

(..... ,) and (..... ,) and (..... ,) [4]

- (c) Determine which one of these turning points is a maximum.
Justify your answer.

[2]

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